ME 465 - Fall 2001

Due: Wednesday, 8/29/01

Perform the indicated matrix multiplication for each problem. Substitute the angles and dimension values given. Use at most 3 significant digits in your answers.

Show the final answer is valid with a correctly scaled sketch for each problem. Use a scale 1 inch = 1 unit OR 25 mm = 1 unit for all sketches

1. $\boldsymbol{q} = 30$ degrees, $\mathbf{x}_1 = 2$ units, $\mathbf{y}_1 = 3$ units, $\underline{\mathbf{R}} = \begin{bmatrix} \mathbf{x}_0 \\ \mathbf{y}_0 \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \boldsymbol{q} & -\sin \boldsymbol{q} & 0 \\ \sin \boldsymbol{q} & \cos \boldsymbol{q} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{y}_1 \\ 1 \end{bmatrix}$

2. q = -45 degrees, $x_1 = -1$ unit, $y_1 = 4$ units,

$$\underline{\mathbf{R}} = \begin{bmatrix} \mathbf{x}_0 \\ \mathbf{y}_0 \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \boldsymbol{q} & -\sin \boldsymbol{q} & 0 \\ \sin \boldsymbol{q} & \cos \boldsymbol{q} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{y}_1 \\ 1 \end{bmatrix}$$

3.
$$a_1 = -1$$
 unit, $b_1 = -2$ units, $x_1 = 2$ unit, $y_1 = 3$ units,

$$\underline{\mathbf{R}} = \begin{bmatrix} x_0 \\ y_0 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & a_1 \\ 0 & 1 & b_1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix}$$

4. $a_1 = 1$ unit, $b_1 = 2$ units, $x_1 = -1$ unit, $y_1 = 4$ units, $\underline{R} = \begin{bmatrix} x_0 \\ y_0 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & a_1 \\ 0 & 1 & b_1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix}$

5. $\boldsymbol{q} = 30$ degrees, $a_1 = 1$ unit, $b_1 = 2$ units, $x_1 = -1$ unit, $y_1 = 4$ units, $\underline{\mathbf{R}} = \begin{bmatrix} x_0 \\ y_0 \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \boldsymbol{q}_1 & -\sin \boldsymbol{q}_1 & a_1 \\ \sin \boldsymbol{q}_1 & \cos \boldsymbol{q}_1 & b_1 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix}$